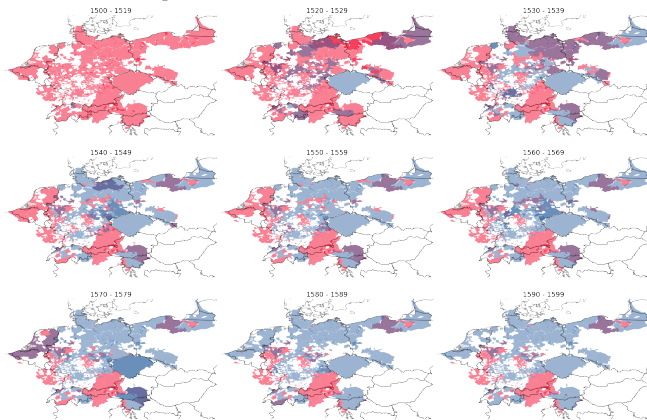


# Path statistics for letter correspondence networks of the European Reformation

Ramona Roller  
21st Juli 2023



# The Adoption of Protestantism



- ▶ 16th-cent. Europe: Holy Roman Empire
- ▶ Territories become protestant
- ▶ Protestant ideas are transmitted

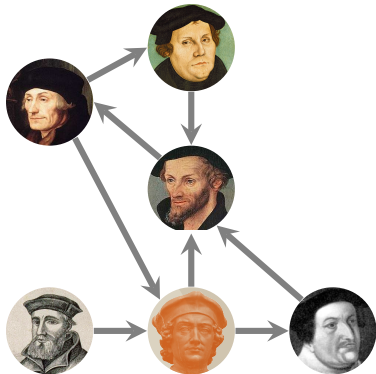
■ Catholic  
■ Protestant

## Research question

How can we characterise the transmission of protestant ideas?

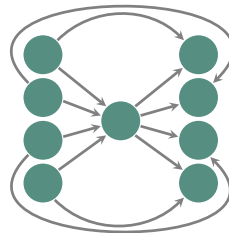
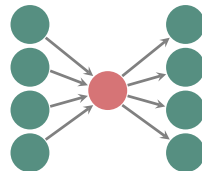
- ▶ Important reformers

# Letter Correspondence Networks for the Transmission of Ideas



- ▶ Nodes: Reformers   Edges: Letters
- ▶  $N_V$ : 3,000    $N_E$ : 30,000
- ✓ sending dates, locations
- Topics, receiving dates

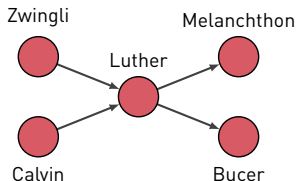
➔ Use node betweenness to identify important reformers for the transmission of ideas



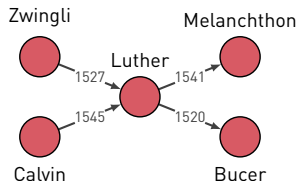
■ High betweenness   ■ Low betweenness

# The Problem

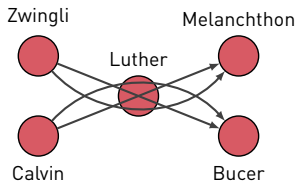
Scholtes, Wider & Garas, 2016



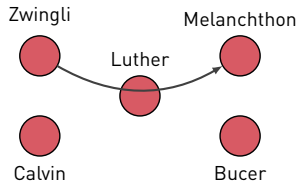
Aggregated network



Add time stamps



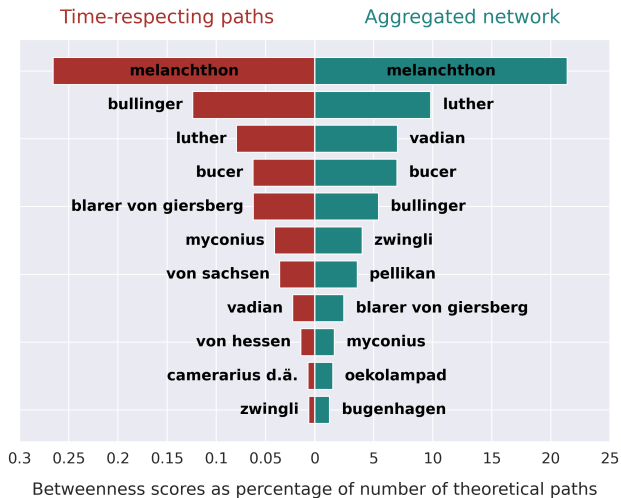
$$btw_{Luther} = 4$$



$$btw_{Luther} = 1$$

- ➔ In aggregated networks information can spread backwards in time
- ➔ Topological network measures in aggregated networks are biased

# Results



- ➔ Melanchthon contributed most
- ➔ Aggregated network overestimate importance of reformers

# Solutions: Account for Time

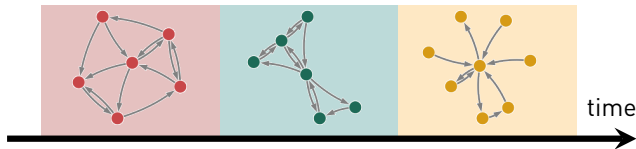
## ▶ **Snapshots**

- ▶ Automatic change points

Darst et al., 2016; Peixoto & Gauvin, 2018

- ▶ Theoretical all of us, I assume

- ▶ Macro and meso scale



## ▶ **Correlations between consecutive node pairs**

- ▶ Time-respecting paths Pfützner et al., 2013

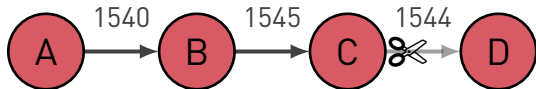
- ▶ Micro scale



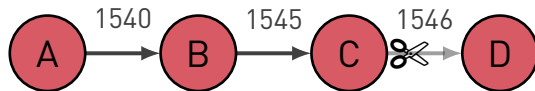
➔ Snapshots and time-respecting paths represent times at different scales: macro vs micro

# Time-respecting Paths Pfitzner et al., 2013

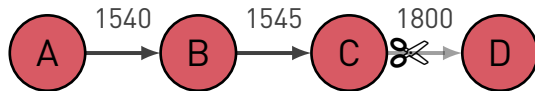
- 1 Sequence of nodes that are connected by time-consecutive edges (**chronology**)..
- 2 ..with the inter-edge time being restricted by a lower (**minimum reaction time**) and an upper bound (**memory**)



1. Chronology is broken



2a. Inter-edge time < minim reaction time



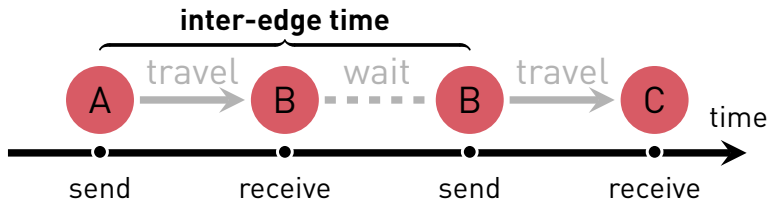
2b. Inter-edge time > memory

## Assumptions

- 1 Time-consecutive edges deal with the same topic
- 2 Time scale is global

- ➔ Accounting for chronology is easy, choosing the correct inter-edge time is not
- ➔ Time scale at which temporal edges influence each other is unknown

# Inter-edge Time for Letters



- ✓ Minimum inter-edge time: 1 day (min. reaction time)
- ❓ Maximum inter-edge time:  $\delta t$  (memory)

## Real life

- ▶ Only waiting time is relevant
  - ▶ Refresh memory: Repeatedly read letter
  - ▶ Continuous waiting  $\uparrow$   $\rightarrow$  Forgetting  $\uparrow$
- ➔ Estimating  $\delta t$  from data is hard

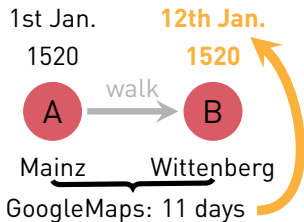
## Data

- ▶ Missing receiving dates: cannot disentangle travel and waiting times
- ▶ No data on repeated reading
- ▶ Total waiting  $\uparrow$   $\rightarrow$  Forgetting  $\uparrow$

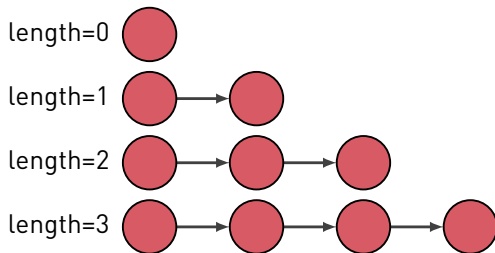


# Estimating $\delta t$ from data

## Waiting time

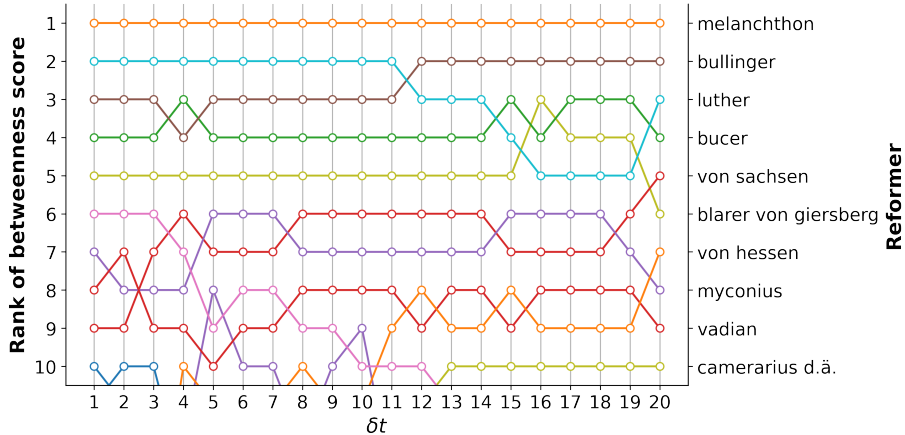


## Path lengths Petrovic, Wagner & Scholtes, 2023



- ▶  $\delta t$  = typical (travel + waiting time)
- ▶ Keep 1% of reformers, 24% of edges
- ➔ Not representative to draw conclusion
- ➔ Sparseness poses problems to data-driven approaches
- ▶ Optimal  $\delta t$ : only one path length dominates
- ▶ No paths for some lengths  $\rightarrow$  no variation for statistical inference
- ➔ Measure is not informative

# Robustness Checks



- ➔ Robust result: Melanchthon is always the most important reformer
- ➔ But other reformers change their scores

# Summary

- ▶ **Aggregated network ignore time**
  - ▶ Information spreads backwards in time
  - ▶ Biased topological network measures
- ▶ **Time-respecting paths**
  - ▶ Temporal ordering of edges
  - ▶ Challenge: parameter calibration ( $\delta t$ )
  - ▶ Calibration methods: problem with data sparseness
  - ▶ Strict assumptions
- ▶ **Outlook**
  - ▶ Validate topological paths with topic-based paths

